Subject:	Result Value paragraph of 13.7.64 GAMMA is wrong
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Reference:	08-007r2

- 1 The Result Value paragraph of 13.7.64 GAMMA has an incomplete definition of the function to be
- 2 computed. The definition applies only for positive arguments, but the function allows negative arguments
- 3 so long as they're not integers.
- 4 The paragraph should read

Result Value. The result has a value equal to a processor-dependent approximation to the gamma function of X,

$$\Gamma(X) = \begin{cases} \int_0^\infty t^{X-1} \exp(-t) \, \mathrm{d}t & X > 0\\ \int_0^\infty t^{X-1} \left(\exp(-t) - \sum_{i=0}^k (-1)^i \frac{t^i}{i!} \right) \, \mathrm{d}t & -k-1 < X < -k, \, k \text{ an integer } > 0 \end{cases}$$

- 5 Note to J3: The formula for X < 0 is called the Cauchy-Saalschütz formula. It can be gotten from the
- 6 one for X > 0 by integrating by parts. See page 44 of Special Functions An Introduction to the
- 7 Classical Functions of Mathematical Physics by Nico Temme.